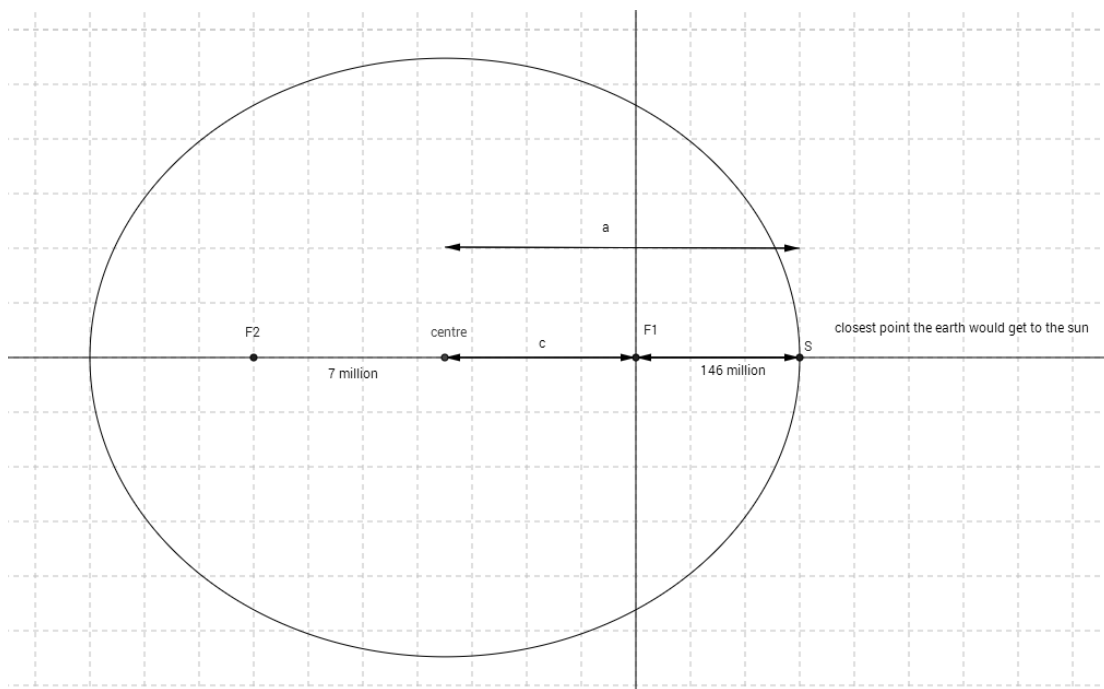


Earth



$F_1 = (0,0)$ $F_2 = (-7 \times 10^6, 0)$ The foci are at $(c,0)$ and $(-c,0)$

$$2c = 7 \times 10^6 \quad c = 3.5 \times 10^6 \text{ km}$$

c = distance from centre to focus, a = distance from centre to vertex/x-intercept

$$c + 146 \times 10^6 = a = 3.5 \times 10^6 + 146 \times 10^6 = 149.5 \times 10^6 \text{ km (3sf)}$$

$$b^2 = a^2 - c^2$$

$$b = \sqrt{(a^2 - c^2)} = \sqrt{[(149.5 \times 10^6)^2 - (3.5 \times 10^6)^2]} = 149 \times 10^6 \text{ km (3sf)}$$

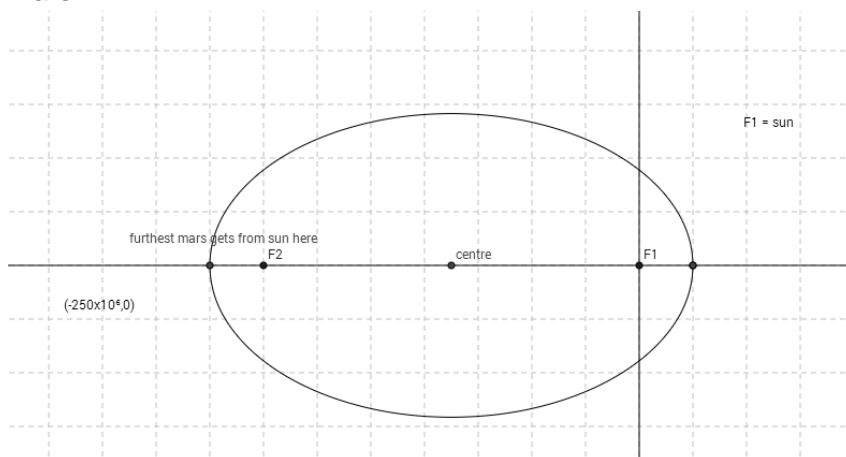
The centre is $3.5 \times 10^6 \text{ km}$ from F_1 so the centre is at $(-3.5 \times 10^6, 0)$

$$\frac{(x + 3.5 \times 10^6)^2}{(149.5 \times 10^6)^2} + \frac{y^2}{(149 \times 10^6)^2} = 1$$

Intercept = $(0,y)$ so y intercept is when $x = 0$ $y = 149.5 \times 10^6 \text{ km}$

1

Mars



$2a$ is total horizontal distance, a is distance from centre to vertex/x intercept
 c is distance from centre to focus

$$2a = 460 \times 10^6 \quad a = 230 \times 10^6$$

$$250 \times 10^6 = a + c \quad c = 250 \times 10^6 - 230 \times 10^6 = 20 \times 10^6$$

$$b = \sqrt{(a^2 - c^2)} = 229 \times 10^6 \text{ km (3sf)}$$

Centre must be 20×10^6 km from F_1 which means centre is at $(-20 \times 10^6, 0)$

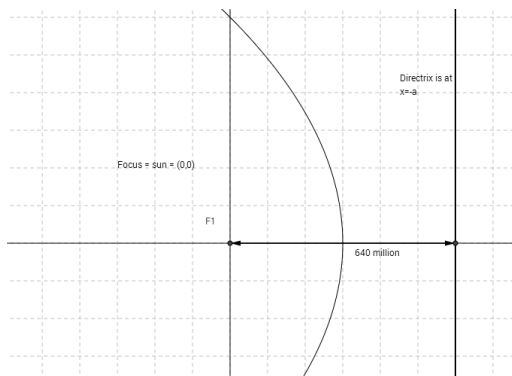
$$\text{Equation: } \frac{(x + 20 \times 10^6)^2}{(230 \times 10^6)^2} + \frac{y^2}{(229 \times 10^6)^2} = 1$$

Asteroid crosses path of Mars at point $(0, y)$ ie when $x = 0$ and $y = ?$

When $x = 0$ $y = 228 \times 10^6 \text{ km (3sf)}$

2

Comet



$$2a = 640 \times 10^6 \quad a = 320 \times 10^6$$

Shift may be 320×10^6 to the right? In which case

$$y^2 = -1280 \times 10^6 (x - 320 \times 10^6)$$

$$y^2 = -1280 \times 10^6 (0 - 320 \times 10^6)$$

$$y = \sqrt{4.096 \times 10^{17}} = 640000000 \text{ km}$$

3